

Trapezoidal Rule:

If f is continuous on $[a, b]$ and if a regular partition of $[a, b]$ is determined by $a = x_0, x_1, x_2, \dots, x_n$, then

$$\int_a^b f(x) dx \approx \frac{b-a}{2n} [f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{n-1}) + f(x_n)]$$

Simpson's Rule:

Suppose f is continuous on $[a, b]$ and n is an even integer.

If a regular partition is determined by $a = x_0, x_1, x_2, \dots, x_{n-1}, x_n = b$, then

$$\int_a^b f(x) dx \approx \frac{b-a}{3n} [f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + \dots + 2f(x_{n-2}) + 4f(x_{n-1}) + f(x_n)]$$

Find the definite integral $\int_0^3 (x^2 + 4)dx$.

a) Using Trapezoidal Rule with $n = 4$,

$$\text{approximate value of } \int_0^3 (x^2 + 4)dx = 21.18$$

b) Using Simpson's Rule with $n = 4$,

$$\text{approximate value of } \int_0^3 (x^2 + 4)dx = 21$$

Find the definite integral $\int_0^1 \frac{1}{(x+7)^2} dx$.

a) Using Trapezoidal Rule with $n = 4$,

$$\text{approximate value of } \int_0^1 \frac{1}{(x+7)^2} dx = 0.017867163338$$

b) Using Simpson's Rule with $n = 4$,

$$\text{approximate value of } \int_0^1 \frac{1}{(x+7)^2} dx = 0.017857157875$$

Find the definite integral $\int_0^{\pi} \sin(x + 5) dx$.

a) Using Trapezoidal Rule with $n = 4$,

$$\text{approximate value of } \int_0^{\pi} \sin(x + 5) dx = 0.537857230583$$

b) Using Simpson's Rule with $n = 4$,

$$\text{approximate value of } \int_0^{\pi} \sin(x + 5) dx = 0.568617801099$$

Find the definite integral $\int_3^4 \cos^2(4x) dx$.

Note: $\int_3^4 \cos^2(4x) dx = \int_3^4 [\cos(4x)]^2 dx$.

a) Using Trapezoidal Rule with $n = 400$,

approximate value of $\int_3^4 \cos^2(4x) dx = 0.591059779758$

b) Using Simpson's Rule with $n = 400$,

approximate value of $\int_3^4 \cos^2(4x) dx = 0.591062815286$