

Recall: $e^{\ln u} = u$; $\ln e^u = u$; $\ln x = \log_e x$; $\ln e = 1$

Solve $e^{\ln 2x} = 18$.

$$e^{\ln 2x} = 18$$

$$2x = 18$$

$$x = 9$$

Solve $e^{3x} = 5$.

Recall: $e^{\ln u} = u$; $\ln e^u = u$; $\ln x = \log_e x$; $\ln e = 1$

$$e^{3x} = 5$$

$$\ln(e^{3x}) = \ln(5)$$

$$3x = \ln 5$$

$$x = \frac{\ln 5}{3}$$

Solve $12 - 3e^x = 6$.

Recall: $e^{\ln u} = u$; $\ln e^u = u$; $\ln x = \log_e x$; $\ln e = 1$

$$12 - 3e^x = 6$$

$$-3e^x = -6$$

$$e^x = \frac{-6}{-3}$$

$$e^x = 2$$

$$\ln(e^x) = \ln(2)$$

$$x = \ln(2)$$

Solve $5e^{-x} = 25$.

Hint: $e^{\ln u} = u$; $\ln e^u = u$; $\ln x = \log_e x$; $\ln e = 1$

$$5e^{-x} = 25$$

$$e^{-x} = 5$$

$$\ln(e^{-x}) = \ln(5)$$

$$-x = \ln 5$$

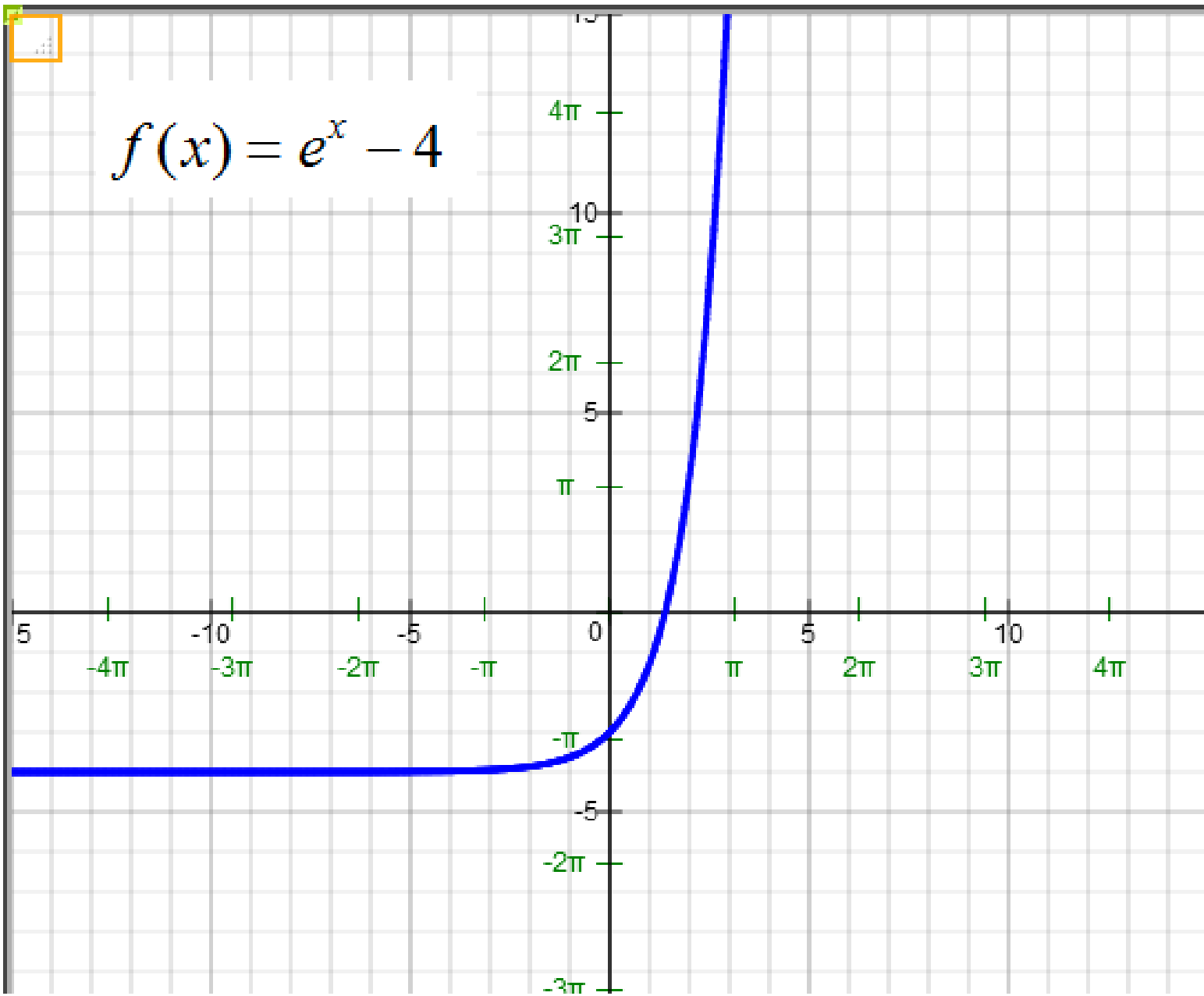
$$x = -\ln 5$$

Graph $f(x) = e^x - 4$

Calculator Input: $y = e^{\wedge}(x) - 4$

a) Domain of $f(x) = (-\infty, \infty)$

b) Range of $f(x) = (-4, \infty)$

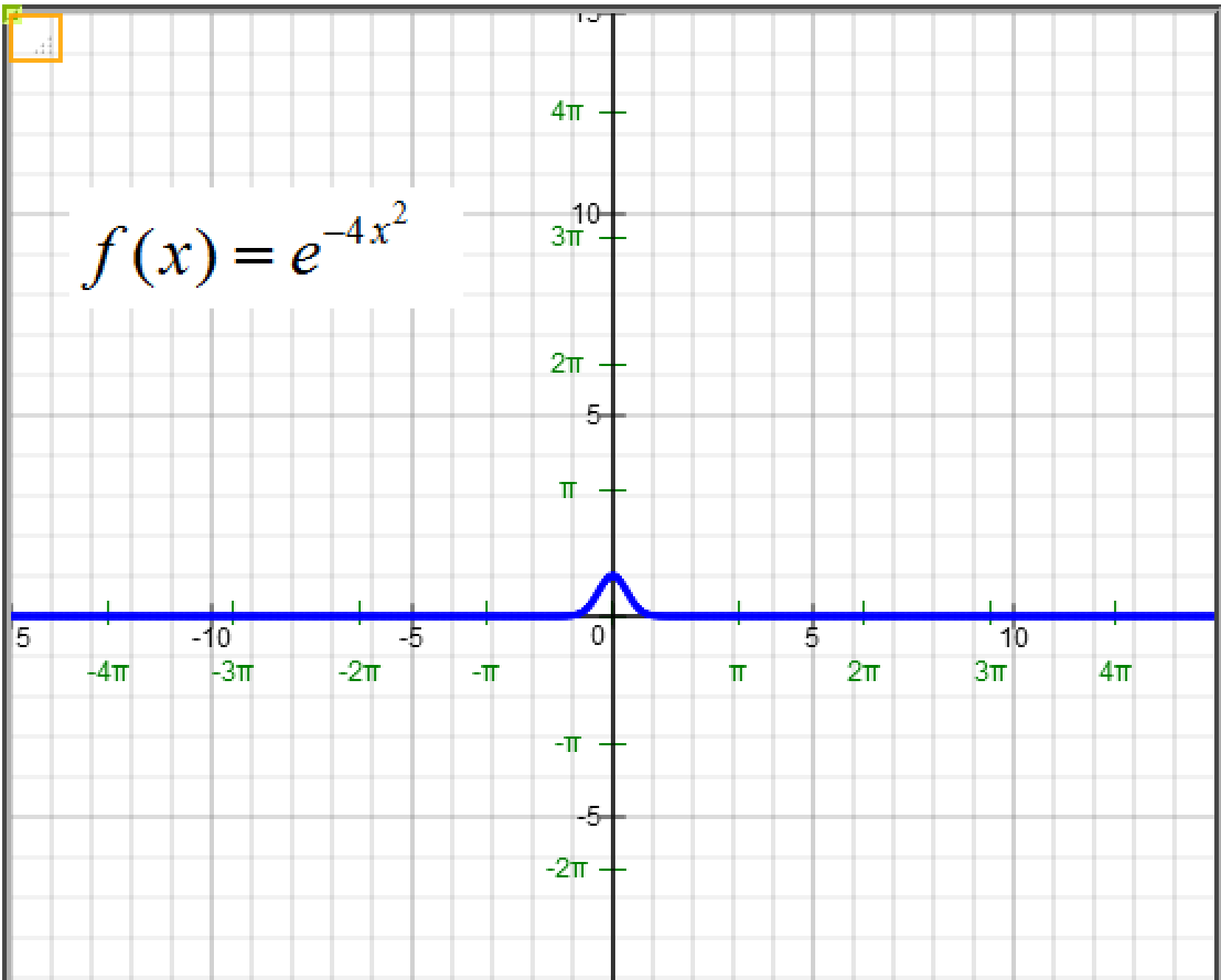


Graph $f(x) = e^{-4x^2}$

Calculator Input: $y = e^{(-4x^2)}$

a) Domain of $f(x) = (-\infty, \infty)$

b) Range of $f(x) = (0, 1]$



Review:

$$1) f(x) = \ln(\text{expression}), \quad f'(x) = \frac{1}{\text{expression}} \cdot D_x(\text{expression})$$

$$2) \int \frac{1}{x} dx = \ln|x| + C; \quad \int \frac{1}{ax+b} dx = \frac{1}{a} \ln|ax+b| + C$$

$$3) f(x) = e^{\text{expression}}, \quad f'(x) = e^{\text{expression}} \cdot D_x(\text{expression})$$

$$4) \int e^x dx = e^x + C; \quad \int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$5) f(x) = \log_b(\text{expression}), \quad f'(x) = \frac{1}{\ln b} \frac{1}{\text{expression}} \cdot D_x(\text{expression})$$

$$6) \int a^x dx = \frac{1}{\ln(a)} a^x + C; \quad \int a^{bx} dx = \frac{1}{b} \frac{1}{\ln(a)} a^x + C$$

Let $y = e^{x-4}$. Find y' .

Recall: For $y = e^{\text{expression}} \Rightarrow y' = \left(e^{\text{expression}} \right) \cdot D_x(\text{expression})$

$$y' = e^{x-4} \cdot D_x(x-4) = e^{x-4} \cdot (1) = e^{x-4}$$

Let $y = 5e^{4x^2+2}$. Find y' .

Recall: For $y = e^{\text{expression}} \Rightarrow y' = \left(e^{\text{expression}} \right) \cdot D_x(\text{expression})$

$$y' = 5e^{4x^2+2} \cdot D_x(4x^2 + 2) = 5e^{4x^2+2} \cdot (8x) = 40xe^{4x^2+2}$$

Let $y = x^2 \cdot e^{2x}$. Find y'

Hint: Use Product Rule for Derivative.

Let F = First Factor; S = Second Factor

Recall: For $y = e^{\text{expression}} \Rightarrow y' = \left(e^{\text{expression}} \right) \cdot D_x(\text{expression})$

$$y' = F \cdot D_x(S) + S \cdot D_x(F)$$

$$y' = (x^2) \cdot D_x(e^{2x}) + (e^{2x}) \cdot D_x(x^2)$$

$$y' = (x^2) \cdot (2e^{2x}) + (e^{2x}) \cdot (2x)$$

Let $y = \frac{2}{e^x + e^{-x}}$. Find y' .

Recall: $y = (\text{expression})^n \Rightarrow y' = n(\text{expression})^{n-1} \cdot D_x(\text{expression})$

Recall: $D_x(e^{\text{power}}) = e^{\text{power}} \cdot D_x(\text{power})$

$$y' = \frac{D \cdot D_x(N) - N \cdot D_x(D)}{D^2}$$

$$y' = \frac{(e^x + e^{-x}) \cdot D_x(2) - 2 \cdot D_x(e^x + e^{-x})}{(e^x + e^{-x})^2}$$

$$y' = \frac{(e^x + e^{-x}) \cdot (0) - 2 \cdot (e^x + -1e^{-x})}{(e^x + e^{-x})^2} = \frac{-2(e^x - e^{-x})}{(e^x + e^{-x})^2}$$

$$\text{Let } y = \frac{3e^x + 1}{4e^x - 1}. \text{ Find } y'$$

Hint: Use Quotient Rule for Derivative.

$$\text{Hint: } D_x(e^{\text{power}}) = e^{\text{power}} \cdot D_x(\text{power})$$

Let N = Numerator Factor; D = Denominator Factor

$$y' = \frac{D \cdot D_x(N) - N \cdot D_x(D)}{D^2}$$

$$y' = \frac{(4e^x - 1) \cdot D_x(3e^x + 1) - (3e^x + 1) \cdot D_x(4e^x - 1)}{(4e^x - 1)^2}$$

$$y' = \frac{(4e^x - 1) \cdot (3e^x) - (3e^x + 1) \cdot (4e^x)}{(4e^x - 1)^2}$$

Let $f(x) = e^{3x} \cdot \ln x$. Find equation of tangent line at $(1, 0)$

Hint: Use Product Rule for Derivative.

Let F = First Factor; S = Second Factor

$$f'(x) = F \cdot D_x(S) + S \cdot D_x(F)$$

$$f'(x) = (e^{3x}) \cdot D_x(\ln x) + (\ln x) \cdot D_x(e^{3x})$$

$$f'(x) = (e^{3x}) \cdot \left(\frac{1}{x}\right) + (\ln x) \cdot (3e^{3x})$$

$$\text{slope of tangent line: } f'(1) = (e^{3x}) \cdot (1/x) + (\ln x) \cdot (3e^{3x})$$

Note: $\ln 1 = 0$

$$= (e^3) \cdot (1) + (0) \cdot (3) = e^3$$

$$\text{Equation of Tangent Line: } y - y_1 = m(x - x_1)$$

$$y - 0 = e^3(x - 1)$$

Let $f(x) = \frac{e^x - e^{-x}}{2} = \frac{1}{2}e^x - \frac{1}{2}e^{-x}$. Find extremums.

$$f'(x) = \frac{1}{2}e^x - \frac{1}{2}(-1e^{-x}) = \frac{1}{2}e^x + \frac{1}{2}(e^{-x})$$

Set $f'(x) = 0$

$$\frac{1}{2}e^x + \frac{1}{2}(e^{-x}) = 0 \quad \Rightarrow \quad e^x + (e^{-x}) = 0$$

Note: $e^x > 0$; $e^{-x} > 0$; $e^x + (e^{-x}) \neq 0$

Therefore, no extremum for $f(x) = \frac{e^x - e^{-x}}{2}$.

Calculator Input: $y = 0.5e^x - 0.5e^{-x}$

